

Density and viscosity measurement of liquid alloys

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➔ Goal

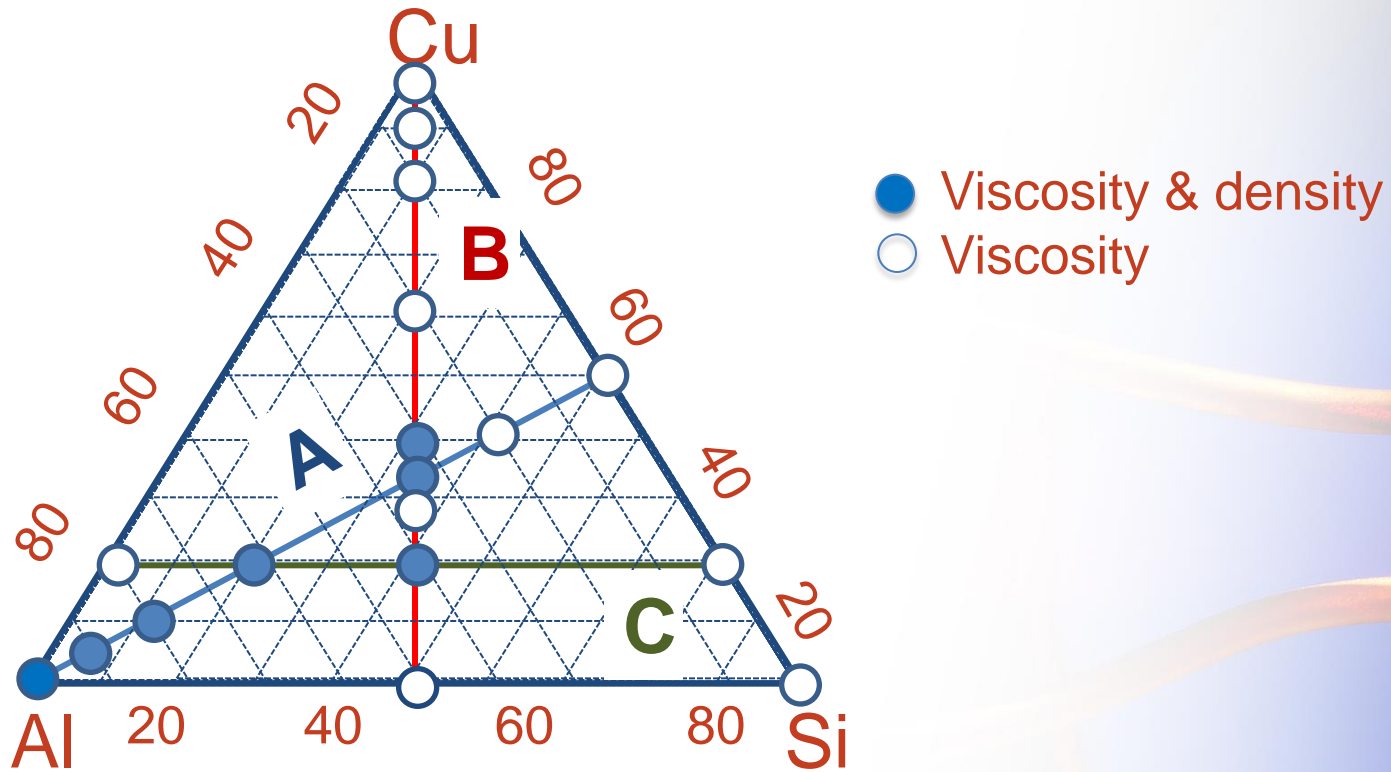
Establishment of the link between thermodynamic and thermophysical properties of the liquid phase density, viscosity and surface tension

Thermodynamic properties	Thermophysical properties
Molar volume: V	Density
Excess Gibbs energy: ${}^E G$	Viscosity
	Surface tension

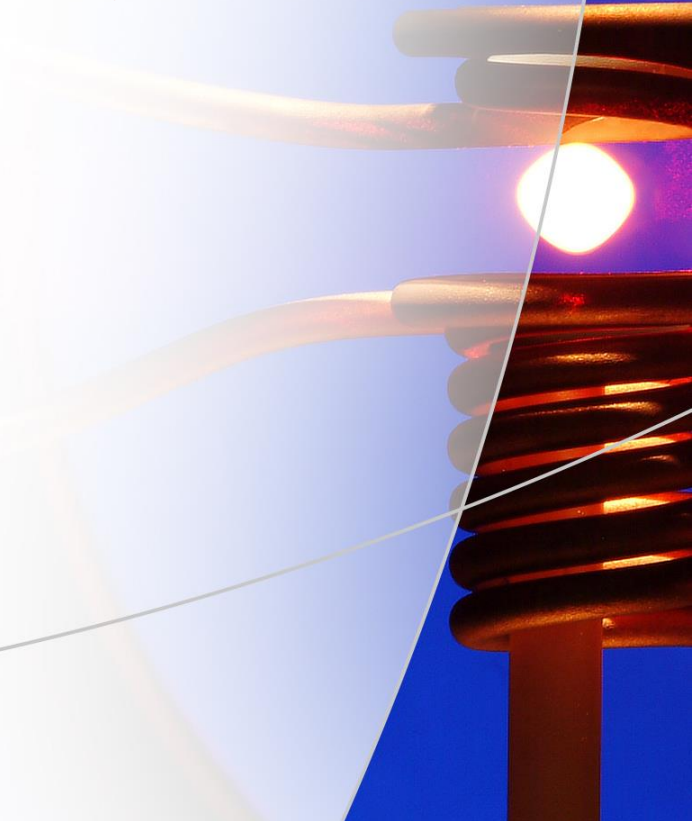


➔ Al-Cu-Si

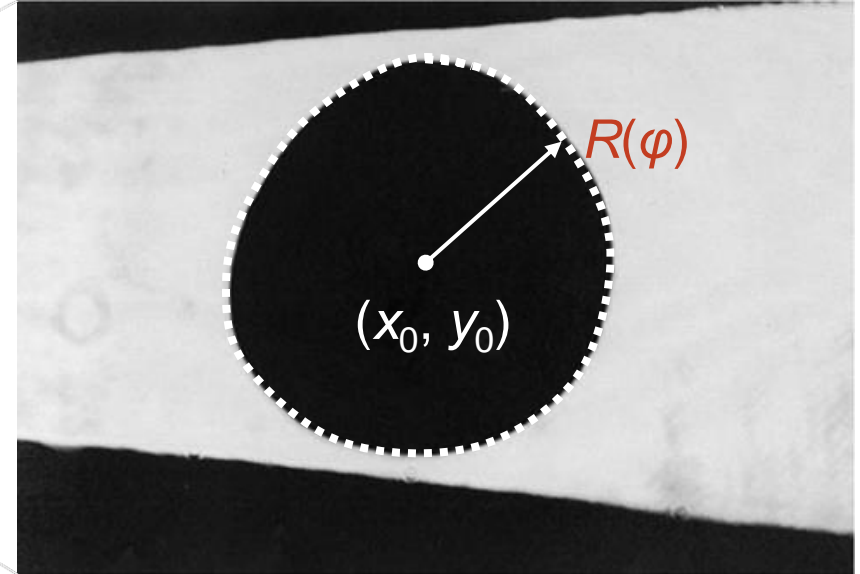
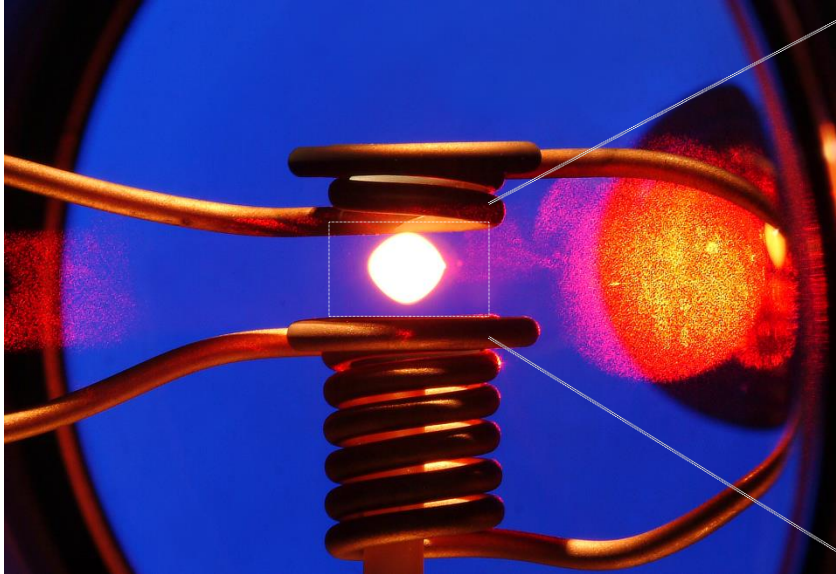
investigated compositions for density and viscosity



measurements carried out in the Al-rich corner



➔ Density measurement



Containerless processing can achieve

- high temperatures and
- investigation of highly reactive materials

Edge fit using Legendre polynomial

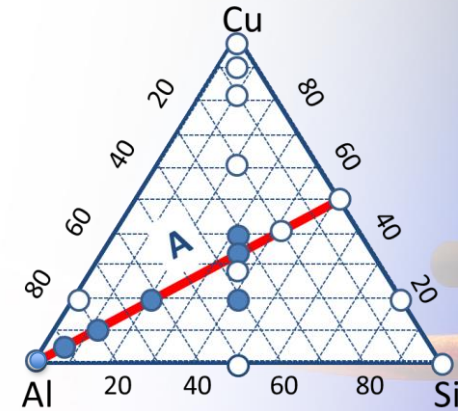
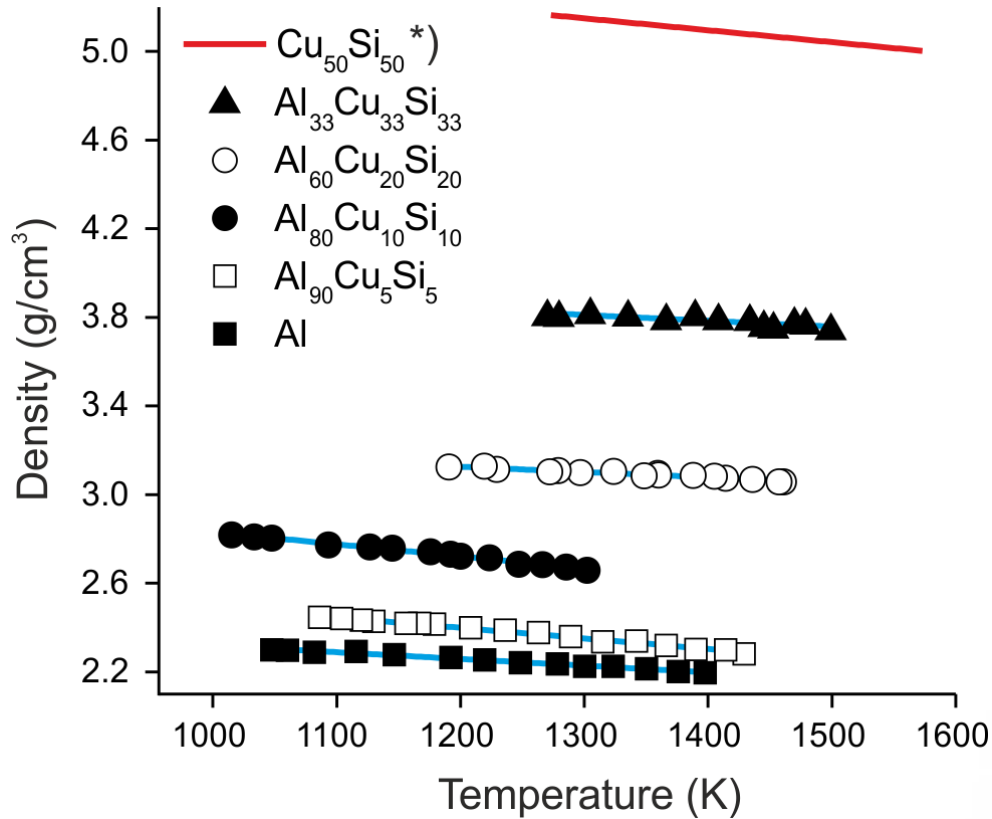
$$\langle R(\varphi) \rangle = \sum_{i=0}^6 a_i P_i(\cos(\varphi))$$

Volume calculation

$$V_P = \frac{2}{3} \pi \int_0^{\pi} \langle R(\varphi) \rangle^3 \sin(\varphi) d\varphi$$

$$(\Delta\rho/\rho \approx \pm 1\%)$$

➔ Al-Cu-Si - density



ρ is linear in temperature over $T_L < T < T_L + 500$ K

*) Adachi, Schick, Brillo, Egry Watanabe, J. Mater. Sci. 45 (2010)

➔ Molar volume ($V = M / \rho$) of a mixture

Ideal volume

$$V_{ideal} = \sum c_i V_i$$

Real volume

$$V_{real} = V_{ideal} + \Delta V$$

Simple expression

$$\Delta V = \sum_i^2 \sum_{i < j}^3 c_i c_j V^{i,j} + c_1 c_2 c_3^T V$$

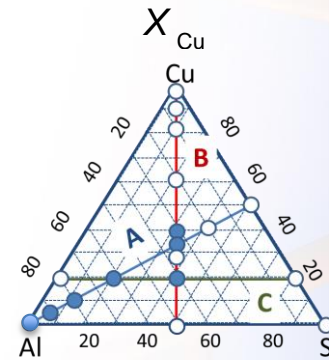
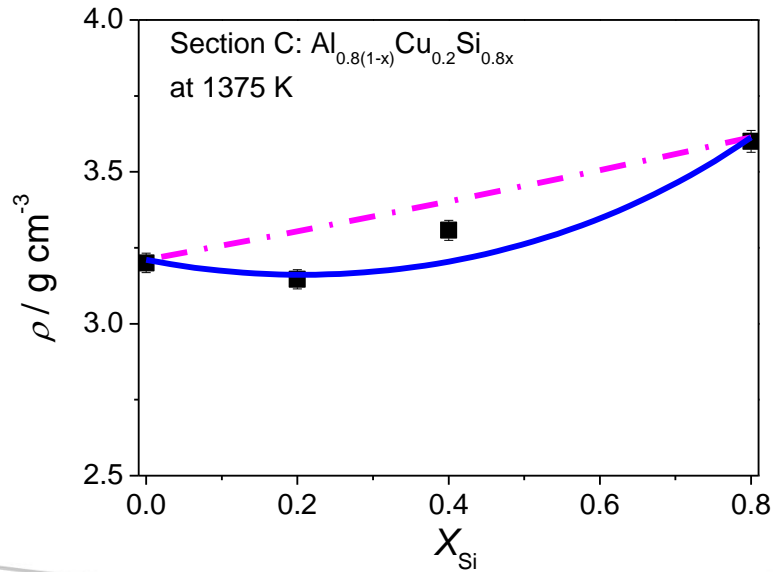
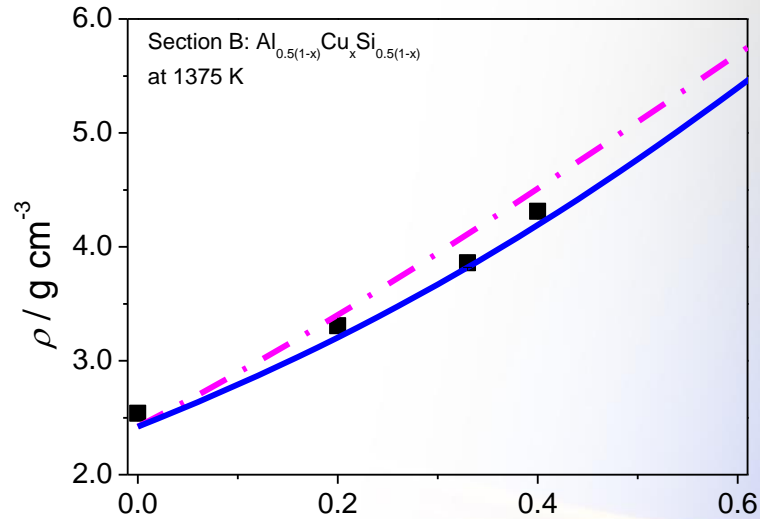
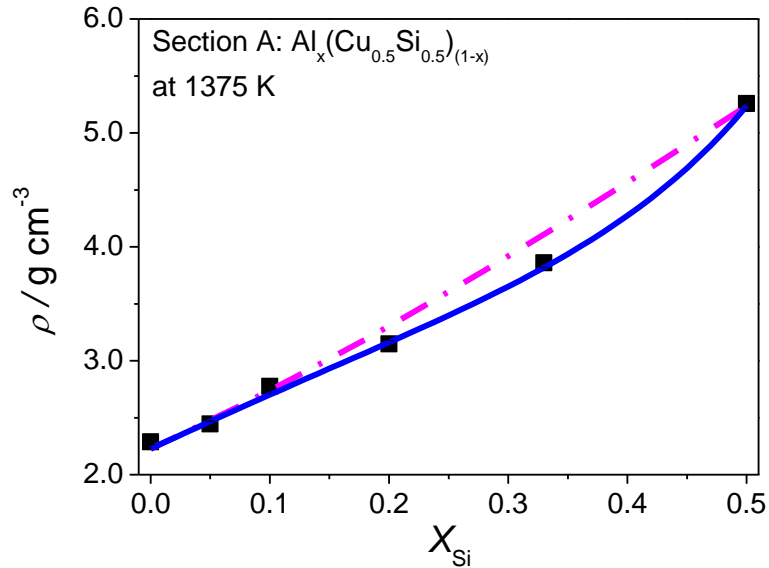
For binary systems: $V^{Al, Cu} = -3.87$ ¹⁾, $V^{Cu-Si} = -2,38$ ²⁾, $V^{Al-Si} = 0$ ³⁾,
(unit: $\text{cm}^3\text{mol}^{-1}$)

For ternary Al-Cu-Si = ?

1) Brillo, Egrý, Westphal, Int. J. Mat. (2008), 2) Adachi, Schick, Brillo, Egrý Watanabe, J. Mater. Sci. (2010)

3) Brillo Egrý, Jap J. Apple Phy. (2011)

Al-Cu-Si – isothermal density

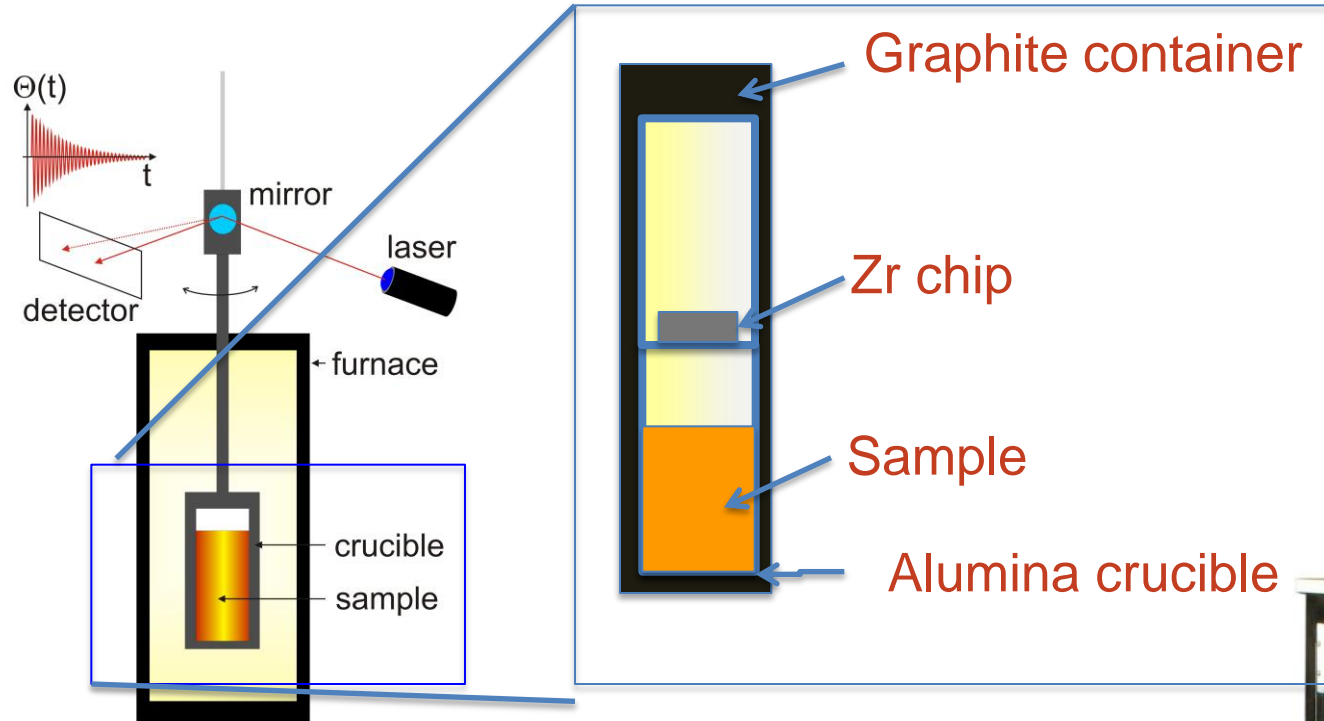


— $T V = 19.7 \text{ cm}^3 \text{ mol}^{-1}$
- - - $T V = 0$

For ternary Al-Cu-Si: $T V = 19.7$

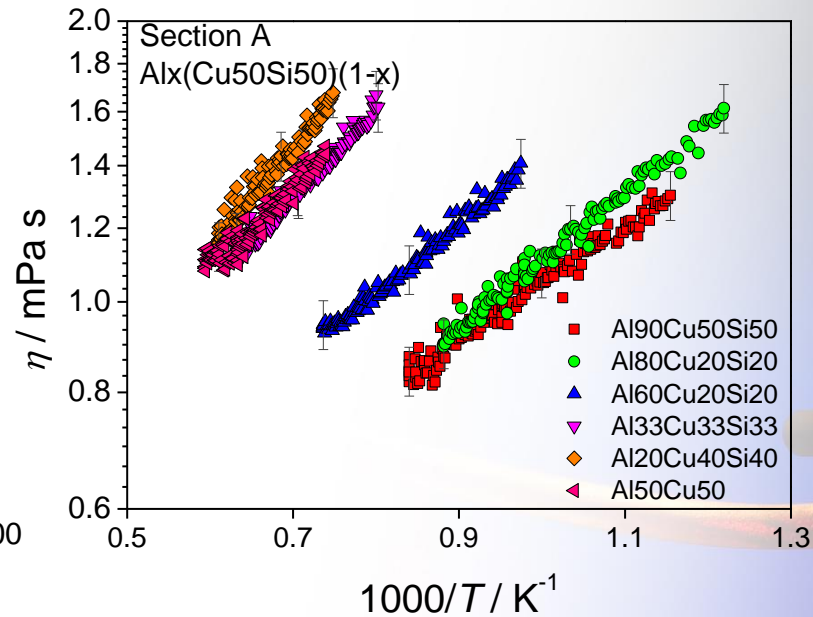
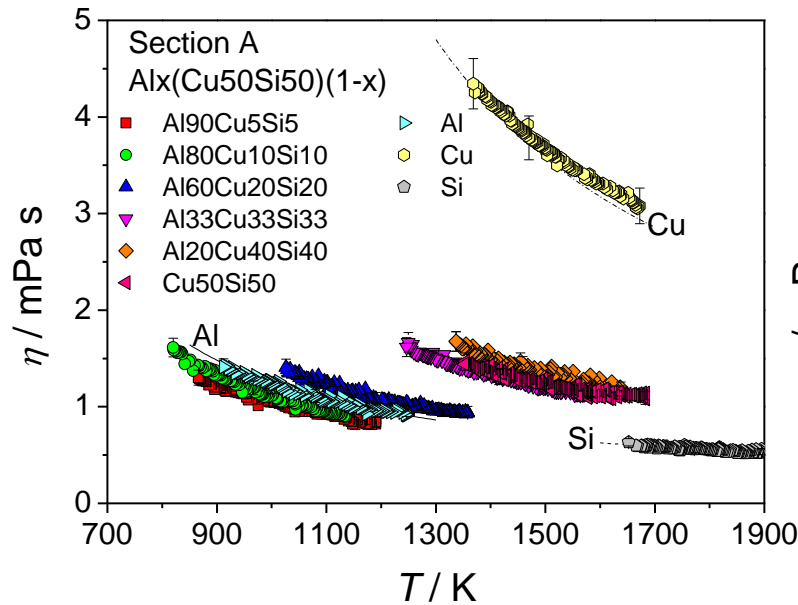
➔ Viscosity measurement

oscillating cup method

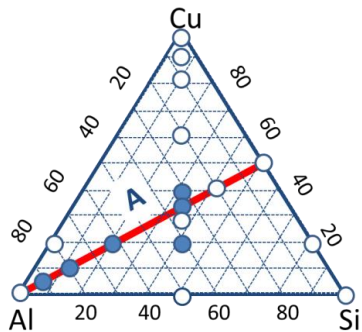


- measurements up to 2300 K
- smooth continuous curves are obtained
- crucible – melt interaction must be considered

➔ Viscosity of liquid Al-Cu-Si



Al: Brillo et al. (2007), Cu: Iida and Guthrie (1993), Si: Sato et al. (2003)



Precise data for entire composition range

Broad T-range: $T_L < T < 1900$ K

Viscosity can be expressed with Arrhenius form

$$\text{(Arrhenius: } \ln(\eta) = \ln(\eta_\infty) + E/RT)$$

➔ Models for the viscosity of liquid alloys

Kaptay ¹⁾

$$\eta = \frac{hN_A}{V} \exp \left(\frac{\sum_i x_i \cdot \Delta E_{A,i} - 0.155 \Delta H_{mix}}{RT} \right)$$

Kozlov et al. ²⁾

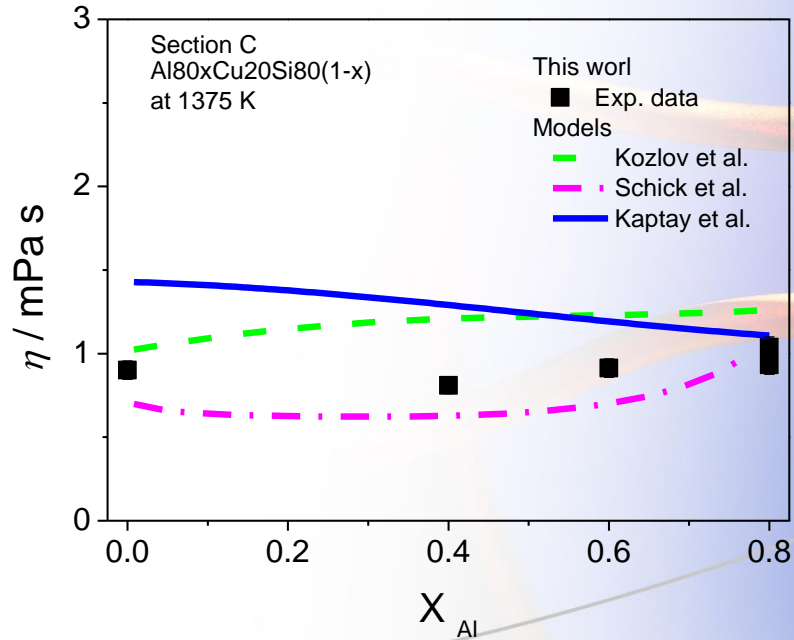
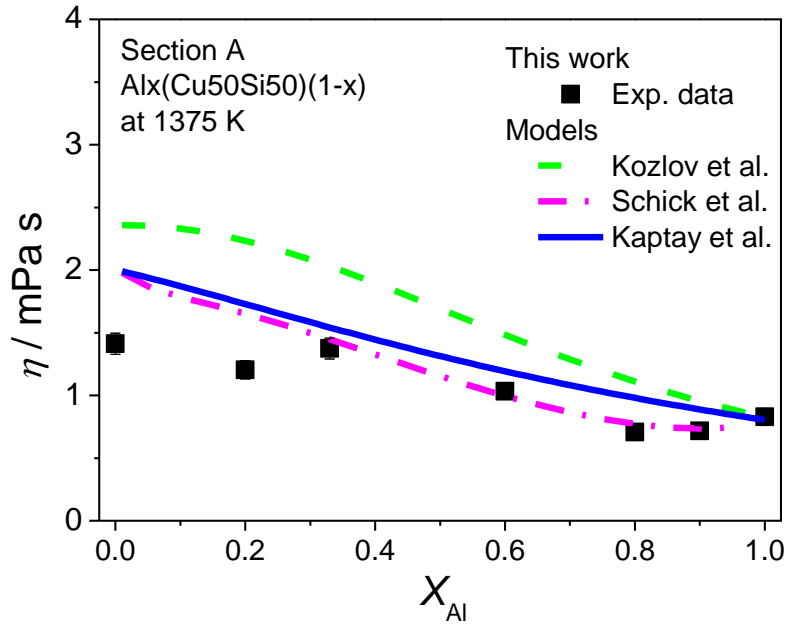
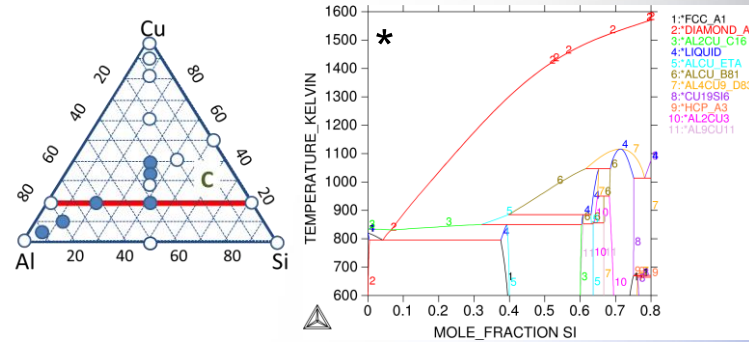
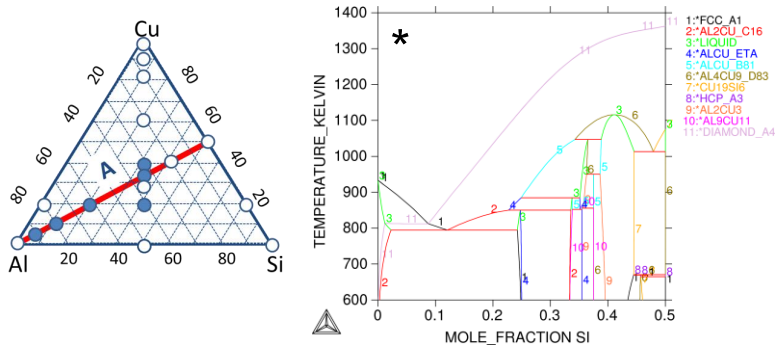
$$\ln \eta = \sum_{i=1}^N x_i \ln \eta_{i,\infty} + \frac{\sum_{i=1}^N x_i \cdot E_i - \Delta H_{mix} / 3}{RT}$$

Schick et al. ³⁾

$$\ln \eta = \sum_{i=1}^N x_i \ln x_i \eta_{i,\infty} + \frac{\sum_{i=1}^N x_i \cdot E_i - \Delta H_{mix}}{RT}$$

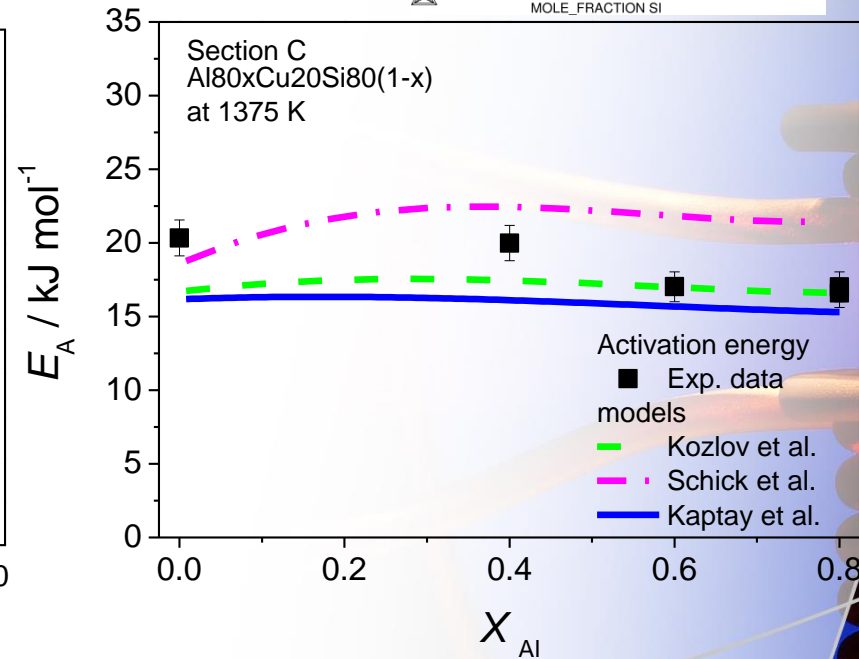
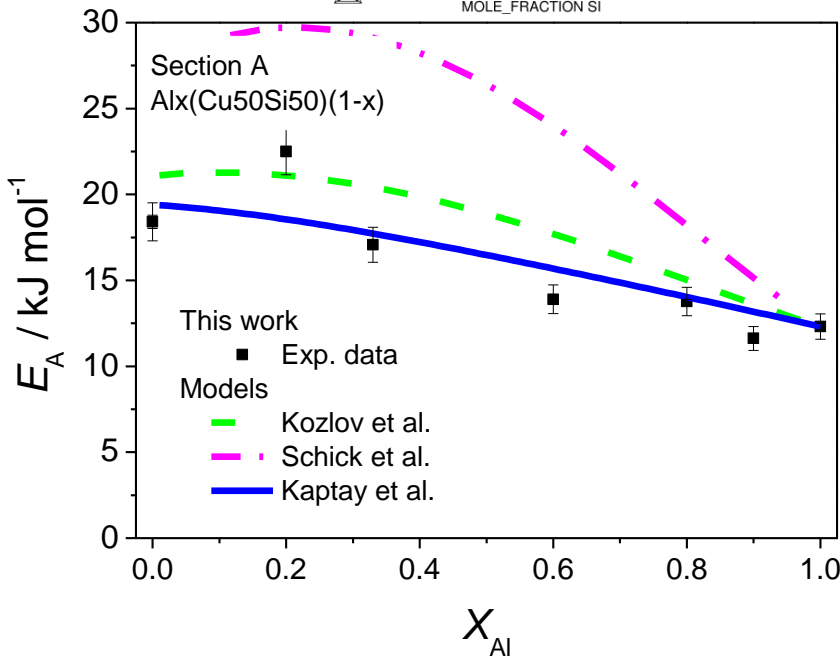
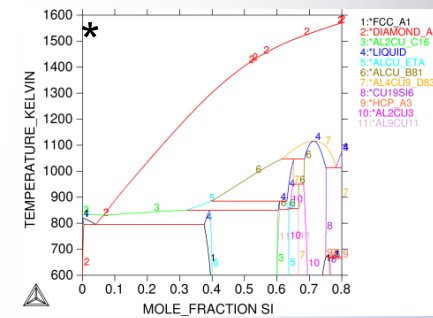
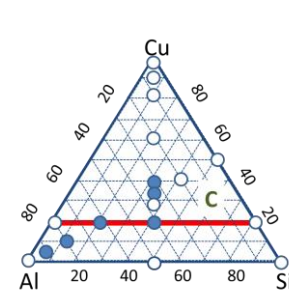
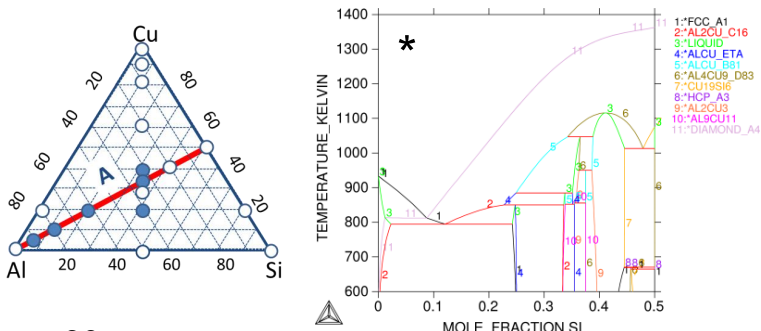
Which model can explain the experimental results?

➔ Viscosity of liquid Al-Cu-Si



* Calculated by Dr. Bengt Hallstedt

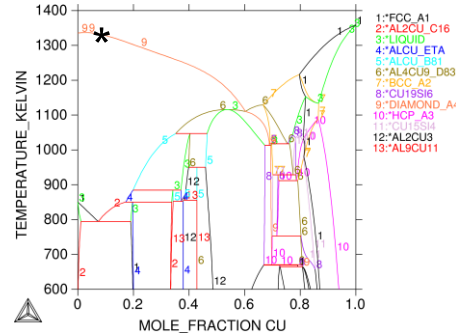
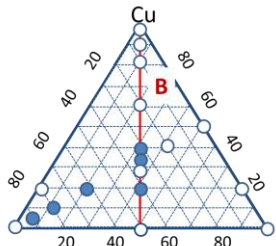
➔ Activation energy of viscous flow for Al-Cu-Si liquid



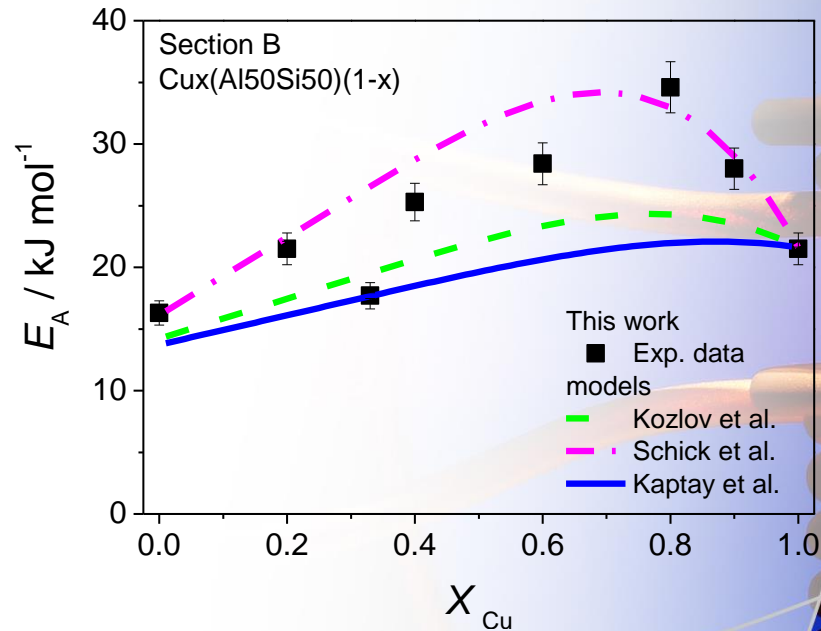
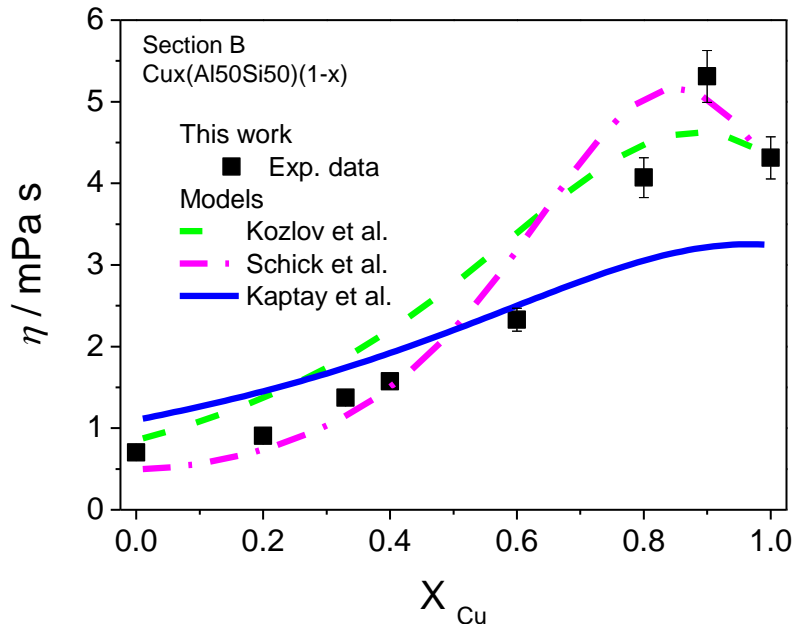
Kaptay model well explains the viscosity along section A and C

$$\eta = \frac{hN_A}{V} \exp\left(\frac{\sum_i x_i \cdot \Delta E_{A,i} - \alpha \Delta H_{mix}}{RT}\right)$$

➔ Viscosity and activation energy of viscous flow of liquid Al-Cu-Si



* Calculated by Dr. Bengt



Schick model well explains the viscosity along section B

$$\ln \eta = \sum_{i=1}^N x_i \ln x_i \eta_{i,\infty} + \frac{\sum_{i=1}^N x_i \cdot E_i - \Delta H_{mix}}{RT}$$

➔ Summary

Density of Al-Cu-Si ternary liquid alloys:

- Density has been measured over broad T-range
- Ternary interaction parameter was determined as
 $\tau V = 19.7 \text{ cm}^3 \text{ mol}^{-1}$.

Viscosity of Al-Cu-Si ternary liquid alloys:

- Viscosities measured for entire concentration and broad T-range
- Viscosity can be described by
 - 1) Kaptay model for eutectic system
 - 2) Schick model for CFM like system

Thank you for your attention

Thermophysical properties of Al-Si-Mg-Cu melt
funding by DFG under contract BR 3665/3-1